

Context & Motivation

Ontology

- A formal representation of a particular domain
- Composed of a *terminological component* – TBox
→ Definition of classes and predicates between classes
- Composed of an *assertion component* – ABox
→ Individuals instantiating classes and predicates

Example

The drug *codein* is an individual instantiating the class *Analgesics*

Context & Motivation (2/6)

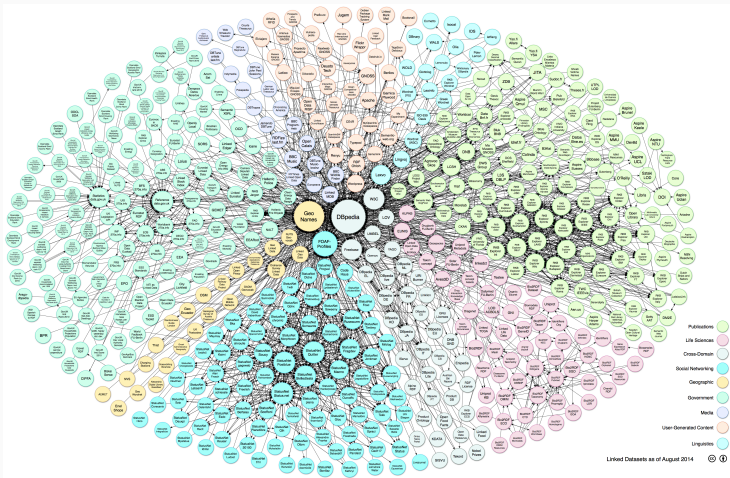


Figure 1: Linked Open Data cloud diagram 2014-08-30, by Andrejs Abele, Paul Buitelaar, Richard Cyganiak, Anja Jentzsch and John P. McCrae.
<http://lod-cloud.net/>

Context & Motivation (3/6)

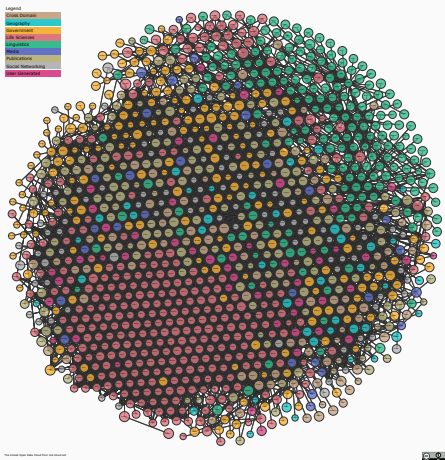


Figure 2: Linked Open Data cloud diagram 2018-06-28, by Andrejs Abele, Paul Buitelaar, Richard Cyganiak, Anja Jentzsch and John P. McCrae.
<http://lod-cloud.net/>

Use Case 1: There is a need for **structure between ontologies**

- Individuals can instantiate classes from several TBoxes
E.g., in the medical domain, MeSH, ICD-9-CM, ICD-10-CM...
- Corresponding classes from several ontologies may be mapped with *equivalence relationships*
- This *alignment* may be a manual review by an expert or a semi-automatic process

Example

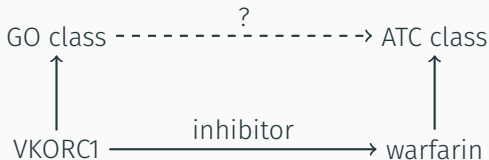
The class **Cardiomyopathies** (D009202) from MeSH is equivalent to **Cardiomyopathy** (425) in ICD-9-CM

Context & Motivation (5/6)

Use Case 2: There is a need for **structure within an ontology**

- In the ABox: predicate assertions, *i.e.*, relations between individuals
E.g., in DrugBank, *VKORC1* is an inhibitor of *warfarin*
- Individuals instantiate classes of ontologies
E.g., GO, ATC
- From predicate assertions, frequently associated classes as domain and range could be discovered
→ Could indicate common behavior at the class level

Example



Context & Motivation (6/6)

Formal Concept Analysis (FCA) [Ganter and Wille, 1999]

- A well-fonded mathematical framework
- Already applied for knowledge engineering purposes

Pattern Structures [Ganter and Kuznetsov, 2001]

- An extension of FCA allowing to have complex descriptions of objects
 - Ontology classes

Concept Annotation [Monnin et al., 2017]

- An extension of FCA introduced in our previous work
- Adding a third dimension to a concept lattice w/o changing its structure
- Already experimented for ontology re-engineering

→ **Combine Concept Annotation and Pattern Structures for the two considered use-cases**

Basics about Ontologies

Considering an ontology \mathcal{O}

- We denote $\mathcal{C}(\mathcal{O})$ the set of classes of \mathcal{O}
- Subsumption relation $C \sqsubseteq D$
→ Partial order between classes
- $\text{lcs}(C_1, C_2)$ is the *least common subsumer* of C_1 and C_2
- Considering a set of classes $\mathcal{C}_n = \{C_1, C_2, \dots, C_n\}$
→ $\text{min } \mathcal{C}_n = \{C \in \mathcal{C}_n \mid \nexists D \in \mathcal{C}_n, D \sqsubseteq C\}$.

Concept Annotation

Concept Annotation: previous work

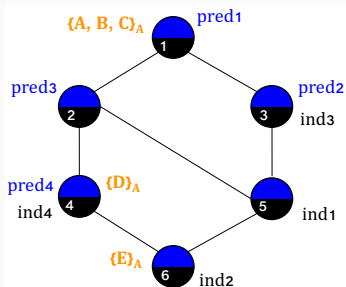
Formal context (G, M, I)

- G : set of **individuals**
- M : set of **predicates**
- $(g, m) \in I$ iff g is involved in a relationship whose predicate is m

Annotation

- Derivation operator $(\cdot)^\diamond : 2^G \rightarrow 2^{C(\mathcal{O})}$
- Given a formal concept (A, B)
$$A^\diamond = \bigcap_{g \in A} \{C \mid \mathcal{O} \models C(g)\}$$

→ Annotated concept (A, B, A^\diamond)



Combining Concept Annotation with Pattern Structures

Objective: only keep as annotation the most specific classes instantiated

Mapping function δ

- $\delta : G \rightarrow 2^{\mathcal{C}(\mathcal{O})}$
- $\delta(g) = \min \{C \mid \mathcal{O} \models C(g)\}$

Similarity operator \sqcap

- Given $g_1, g_2 \in G$
- $\delta(g_1) \sqcap \delta(g_2) = \min \{\text{lcs}(C_1, C_2) \mid \forall (C_1, C_2) \in \delta(g_1) \times \delta(g_2)\}$

Derivation operator $(\cdot)^\circ$

- $(\cdot)^\circ : 2^G \rightarrow 2^{\mathcal{C}(\mathcal{O})}$
- Given a formal concept (A, B) , $A^\circ = \prod_{g \in A} \delta(g)$

Use Case 1: Suggesting Mappings between Classes of Ontologies

Suggesting Mappings between Classes of Ontologies (1/4)

Running Example

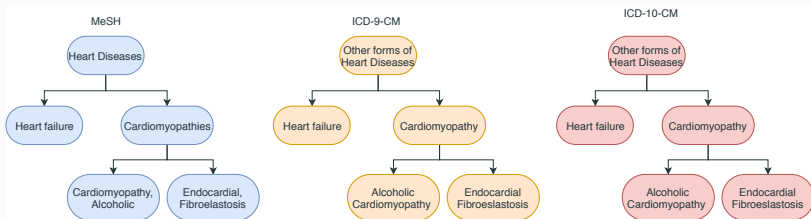
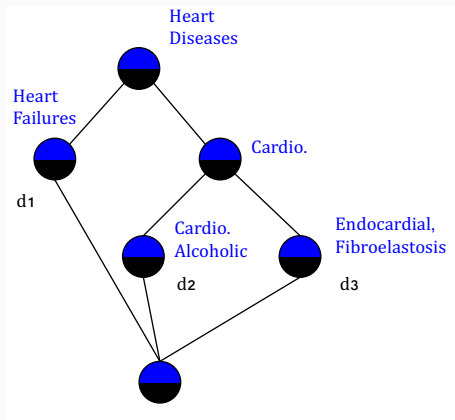


Figure 3: TBoxes

	\mathcal{O}_{ref} (MeSH)	\mathcal{O}_1 (ICD-9-CM)	\mathcal{O}_2 (ICD-10-CM)
d1	Heart failure	Heart failure	Heart failure
d2	C., Alcoholic	Alcoholic C.	Alcoholic C.
d3	E., Fibroelastosis	E. Fibroelastosis	E. Fibroelastosis

Table 1: Classes instantiated by the individuals (d1, d2, d3) of the ABox

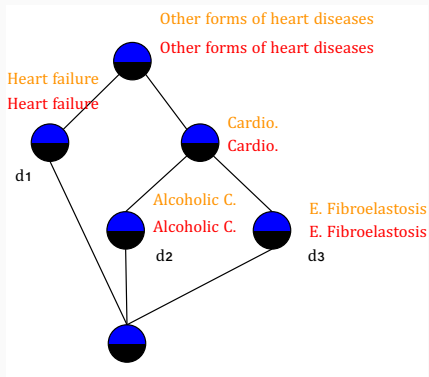
Suggesting Mappings between Classes of Ontologies (2/4)



Classifying individuals w.r.t. \mathcal{O}_{ref}

- Pattern Structure $(G, (2^{\mathcal{C}(\mathcal{O}_{ref})}, \Pi_{ref}), \delta_{ref})$
- Pattern Concepts (A, D) with $A \subseteq G$ and $D \in 2^{\mathcal{C}(\mathcal{O}_{ref})}$

Suggesting Mappings between Classes of Ontologies (3/4)



Annotating with \mathcal{O}_1 and \mathcal{O}_2

- Two annotations for a formal concept (A, B)
 - w.r.t. \mathcal{O}_1

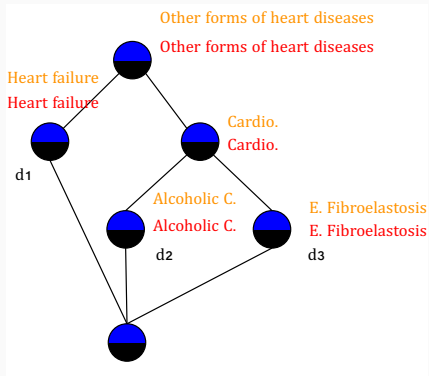
$$A^{\mathcal{O}_1} = \prod_{g \in A} \delta_1(g)$$

- w.r.t. \mathcal{O}_2

$$A^{\mathcal{O}_2} = \prod_{g \in A} \delta_2(g)$$

→ Annotated concept
 $(A, B, A^{\mathcal{O}_1}, A^{\mathcal{O}_2})$

Suggesting Mappings between Classes of Ontologies (4/4)



Reading mappings from the annotated lattice

Considering an annotated concept $(A, B, A^{\circ_1}, A^{\circ_2})$

- $A^{\circ_1} \subseteq \mathcal{C}(\mathcal{O}_1)$
- $A^{\circ_2} \subseteq \mathcal{C}(\mathcal{O}_2)$

Considering each pair $(C_1, C_2) \in A^{\circ_1} \times A^{\circ_2}$

- They are instantiated by all individuals in A
- Suggestion of $C_1 \Leftrightarrow C_2$

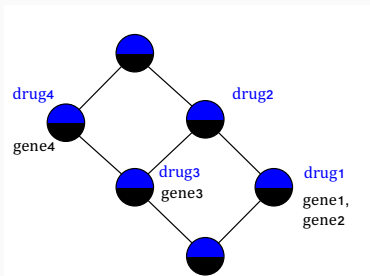
Use Case 2: Discovering Associated Classes as Domain and Range of a Predicate

Running example

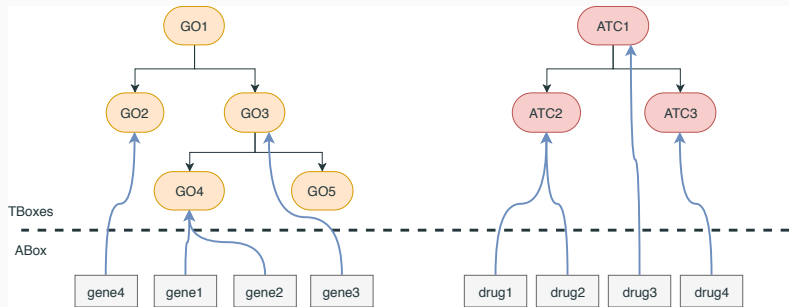
- A set G of individuals instantiating classes of an ontology \mathcal{O}_1
→ genes instantiating classes of GO
- A set M of individuals instantiating classes of an ontology \mathcal{O}_2
→ drugs instantiating classes of ATC
- The incidence relation $I \subseteq G \times M$ indicates that an individual from G is in a relationship with an individual from M
→ the gene is an inhibitor of the drug

Discovering Associated Classes as Domain and Range (2/5)

	<i>drug₁</i>	<i>drug₂</i>	<i>drug₃</i>	<i>drug₄</i>
<i>gene₁</i>	×	×		
<i>gene₂</i>	×	×		
<i>gene₃</i>		×	×	×
<i>gene₄</i>				×



Discovering Associated Classes as Domain and Range (3/5)



Discovering Associated Classes as Domain and Range (4/5)

Annotating with \mathcal{O}_1 and \mathcal{O}_2

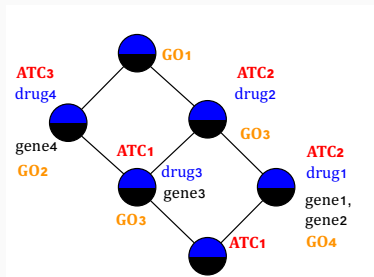
- Two annotations for a formal concept (A, B)
 - w.r.t. \mathcal{O}_1

$$A^{\mathcal{O}_1} = \prod_{g \in A} \delta_1(g)$$

- w.r.t. \mathcal{O}_2

$$B^{\mathcal{O}_2} = \prod_{m \in B} \delta_2(m)$$

→ Annotated concept $(A, B, A^{\mathcal{O}_1}, B^{\mathcal{O}_2})$

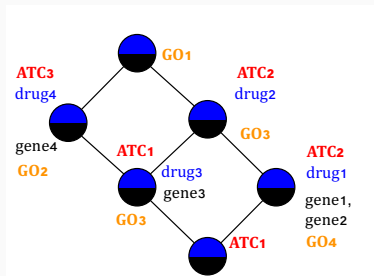


Discovering Associated Classes as Domain and Range (5/5)

Reading Domain and Range from the annotated lattice

- Considering an annotated concept (A, B, A^{o_1}, B^{o_2})
- Every individual in A is in relationship w/ every individual in B
- $A^{o_1} \subseteq \mathcal{C}(\mathcal{O}_1)$ is the set of the most specific classes instantiated by all individuals in A
- $B^{o_2} \subseteq \mathcal{C}(\mathcal{O}_2)$ is the set of the most specific classes instantiated by all individuals in B

→ Classes from A^{o_1} as domain are associated with classes from B^{o_2} as range



Conclusion & Perspectives

Conclusion & Perspectives

- Pattern structures enable more complex annotations
- The resulting lattice can be seen as a *pivot* structure
- The approach needs to be validated on real data sets
- Mappings suggestion
 - Closed World Assumption vs Open World Assumption
 - Choice of background knowledge \mathcal{O}_{ref} ?
 - Potential other applications: concept drift...
- Discovering associated classes as domain and range
 - Interactive exploration of the annotated lattice
 - Add metrics (*e.g.*, *support*) for selecting interesting associations?

Thank you for your attention
Questions?



Ganter, B. and Kuznetsov, S. O. (2001).

Pattern Structures and Their Projections.

In Conceptual Structures: Broadening the Base, 9th International Conference on Conceptual Structures, ICCS 2001, Stanford, CA, USA, July 30-August 3, 2001, Proceedings, pages 129–142.



Ganter, B. and Wille, R. (1999).

Formal concept analysis - mathematical foundations.

Springer.



Monnin, P., Lezoche, M., Napoli, A., and Coulet, A. (2017).
**Using Formal Concept Analysis for Checking the Structure of an
Ontology in LOD: The Example of DBpedia.**

*In Foundations of Intelligent Systems - 23rd International
Symposium, ISMIS 2017, Warsaw, Poland, June 26-29, 2017,
Proceedings, pages 674–683.*